

$$\textcircled{18} \quad x^{2/3} + y^{2/3} = 1$$

$$y^{2/3} = 1 - x^{2/3}$$

$$y = (1 - x^{2/3})^{3/2}$$

$$\frac{dy}{dx} = \frac{3}{2} (1 - x^{2/3})^{1/2} \left(-\frac{2}{3} x^{-1/3} \right)$$

$$\begin{aligned} (y')^2 &= \frac{9}{4} (1 - x^{2/3}) \cdot \left(\frac{4}{9} x^{-2/3} \right) \\ &= \frac{1 - x^{2/3}}{x^{2/3}} = x^{-2/3} - 1 \end{aligned}$$

$$(y')^2 + 1 = x^{-2/3}$$

$$\sqrt{x^{-2/3}} = x^{-1/3}$$

$$4 \int_0^1 x^{-1/3} dx = 4 \cdot \frac{2}{2} x^{2/3} \Big|_0^1$$

$$= 4 \cdot \frac{3}{2} = 6$$

$$\textcircled{11} \quad y = \frac{1}{4}x^4 \quad [1, 2]$$

$$y' = x^3 \quad (y')^2 = x^6 \quad (y')^2 + 1 = x^6 + 1$$

$$\int_1^2 \sqrt{x^6 + 1} \, dx$$

$$\frac{1}{2} - \frac{1}{5} \left(\sqrt{1^6 + 1} + 2\sqrt{1.2^6 + 1} + 2\sqrt{1.4^6 + 1} + 2\sqrt{1.6^6 + 1} + 2\sqrt{1.8^6 + 1} + \sqrt{2^6 + 1} \right)$$

$$\int \sec x \, dx = \int \sec x \cdot \frac{\sec x + \tan x}{\sec x + \tan x} \, dx$$
$$= \int \frac{\sec^2 x + \sec x \tan x}{\tan x + \sec x} \, dx \quad \int \frac{du}{u}$$

$$u = \tan x + \sec x$$

$$= \ln | \tan x + \sec x |$$