

$$\textcircled{41} \quad G(x) = \int_0^{x^3} \sqrt{t+1} \, dt$$

$f'(2)$

$$G'(x) = \sqrt{x^3+1} \cdot 3x^2$$

$$f'(2) = 3 \cdot 3 \cdot 4 = 36$$

(39)

$$r(t) = 100 + 72t - 3t^2$$

$$\frac{420}{t}$$

$$\int_0^{24} r(t) dt =$$

$$\int_{12}^{24} r(t) dt =$$

$$\textcircled{70} \int_{-4}^{-2} \frac{12x \, dx}{(x^2 + 2)^3}$$

$$u = x^2 + 2$$

$$du = 2x \, dx$$

$$6 \, du = 12x \, dx$$

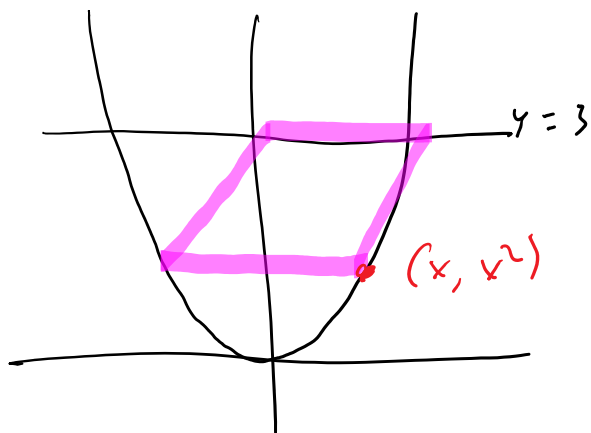
$$6 \int \frac{du}{u^3}$$

$$6 \int u^{-3} \, du = 6 \cdot \frac{u^{-2}}{-2} = \frac{-3}{u^2} \Big|_{10}^6$$

$$= -3 \left(\frac{1}{6^2} - \frac{1}{10^2} \right)$$

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The base of a solid is region enclosed by $y = x^2$ and $y = 3$. The cross-sections \perp to y -axis are squares. Find volume



$$y = x^2 \rightarrow x = \pm \sqrt{y}$$

$$\text{side length} = 2\sqrt{y}$$

$$\text{area of } \square = 4y$$

$$(x, x^2) \text{ or } (\sqrt{y}, y)$$

$$\int_0^3 4y \, dy = 2y^2 \Big|_0^3$$

$$= 18$$