

Calculus Study Guide: 10.1

Determine whether the sequence converges or diverges. If it converges, find its limit.

$$a_n = \frac{e^n}{n^2} \begin{matrix} \infty \\ \infty \end{matrix} \xrightarrow{LR} \frac{e^n}{2n} \begin{matrix} \infty \\ \infty \end{matrix} \rightarrow \frac{e^n}{2} \rightarrow \infty$$

Converges. Limit = _____

Diverges

$$a_n = \sin \frac{\pi(2n-1)}{2} \quad (1, -1, 1, -1)$$

Converges. Limit = _____

Diverges

A sequence is defined recursively as $a_1 = 9$, $a_n = \left(-\frac{2}{3}\right)a_{n-1}$.

$$a_2 = -6$$

$$a_3 = 4$$

$$a_4 = -\frac{8}{3}$$

Converges. Limit = 0

Diverges

$$a_n = \left(\frac{5}{4}\right)^n$$

Converges. Limit = _____

Diverges

$$a_n = \left(\frac{4}{5}\right)^n \rightarrow 0$$

Converges. Limit = 0

Diverges

$$a_n = 4 + (-1)^n$$

3, 5, 3, 5

Converges. Limit = _____

Diverges

Calculate the first 4 terms of the sequence, starting with $n = 1$.

$$b_n = \left(1 + \frac{1}{n}\right)^n \quad b_1 = (2)^1 \quad b_2 = \left(1 + \frac{1}{2}\right)^2 \quad b_3 = \left(1 + \frac{1}{3}\right)^3$$
$$b_4 = \left(1 + \frac{1}{4}\right)^4$$

$$b_1 = \underline{2}$$

$$b_2 = \underline{2.25}$$

$$b_3 = \underline{2.370}$$

$$b_4 = \underline{2.441}$$