

Calculus Study Guide: 10.7

Find the first 3 terms of the Maclaurin polynomial for $g(x) = \frac{1}{1+x} e^x$

$$\begin{aligned} & (1-x+x^2-x^3) \left(1+x+\frac{x^2}{2}+\frac{x^3}{6}\right) \\ & \left(1+x+\frac{x^2}{2}+\frac{x^3}{6}\right) - x - x^2 - \frac{x^3}{2} + x^2 + x^3 - x^3 \\ & 1 + \frac{x^2}{2} - \frac{x^3}{3} \end{aligned}$$

Find the first 4 terms of the Maclaurin series for $h(x) = \frac{1}{1-x^3}$

$$1 + x^3 + x^6 + x^9$$

Use the Maclaurin expansion for e^{-x^2} to express $\int_0^x e^{-t^2} dt$ as an alternating series.

$$e^x = 1 + x + \frac{x^2}{2} + \frac{x^3}{6} + \dots$$

$$e^{-x^2} = 1 - x^2 + \frac{x^4}{2} - \frac{x^6}{6} + \dots$$

$$\int (1 - x^2 + \frac{x^4}{2} - \frac{x^6}{6}) dx = x - \frac{x^3}{3} + \frac{x^5}{10} - \frac{x^7}{42} + \dots \Big|_0^x$$

$$\frac{x^{2n-1}}{(2n-1)(n-1)!}$$

How many terms of the infinite series are needed to approximate the integral for $x=1$ with an error less than 0.001?

$$1 - \frac{1}{3} + \frac{1}{10} - \frac{1}{42} + \frac{1}{192} - \frac{1}{(2n-1)(n-1)!} < 0.001$$

if $n=6$

Include 5 terms
first omitted term = $\frac{1}{7200}$